

# Deep learning:

*Feed-forward (continued) & NNAlign*

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# Recap: Feed-forward Networks (FFNs)

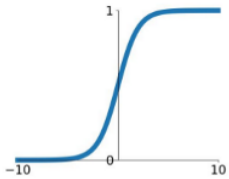
## Keypoints:

- Weights connecting every node together
- **Activation functions** after layers

## Activation Functions

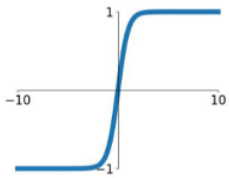
### Sigmoid

$$\sigma(x) = \frac{1}{1+e^{-x}}$$



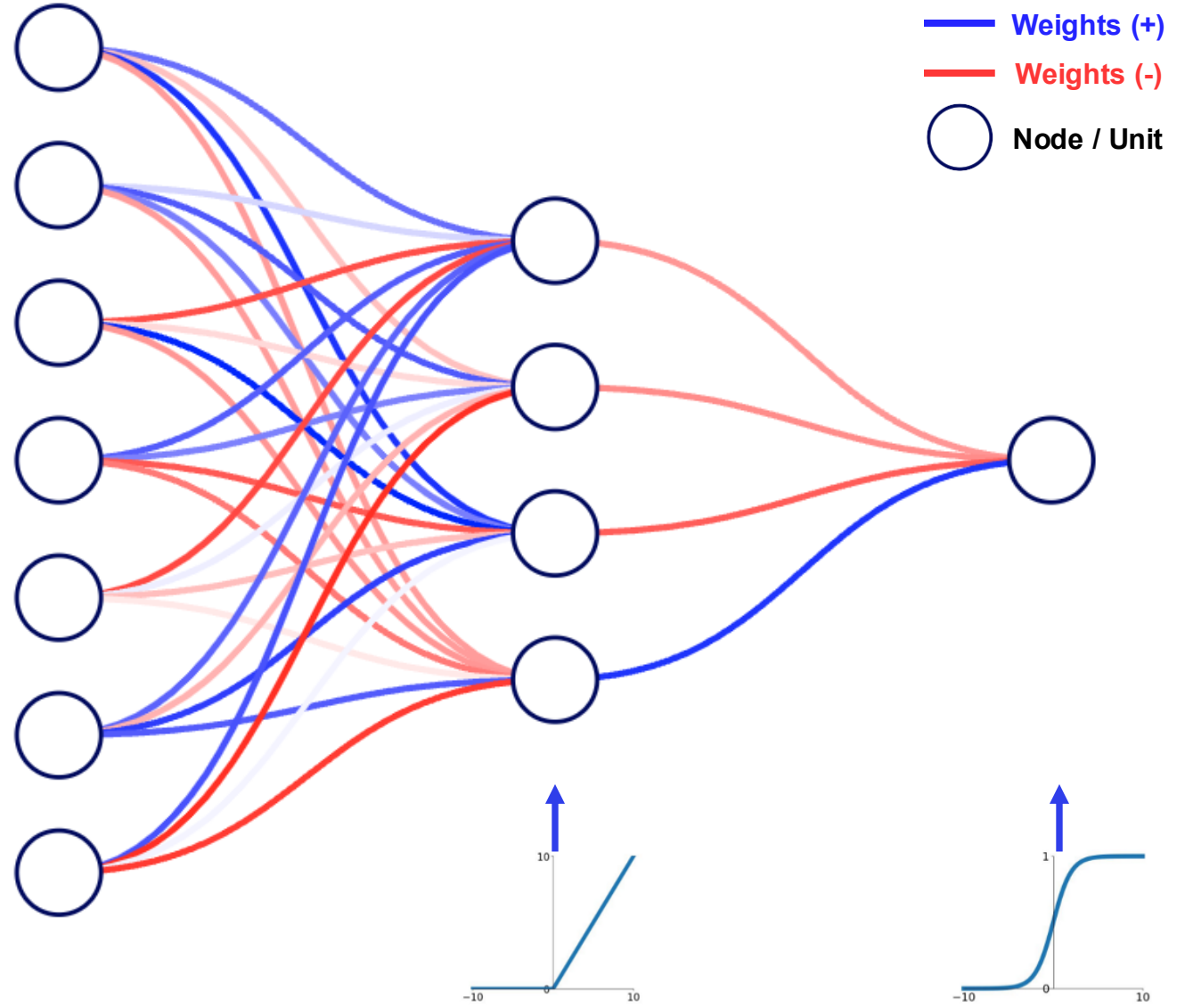
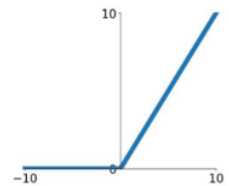
### tanh

$$\tanh(x)$$



### ReLU

$$\max(0, x)$$



Input Layer  $\in \mathbb{R}^7$

Hidden Layer  $\in \mathbb{R}^4$

Output Layer  $\in \mathbb{R}^1$

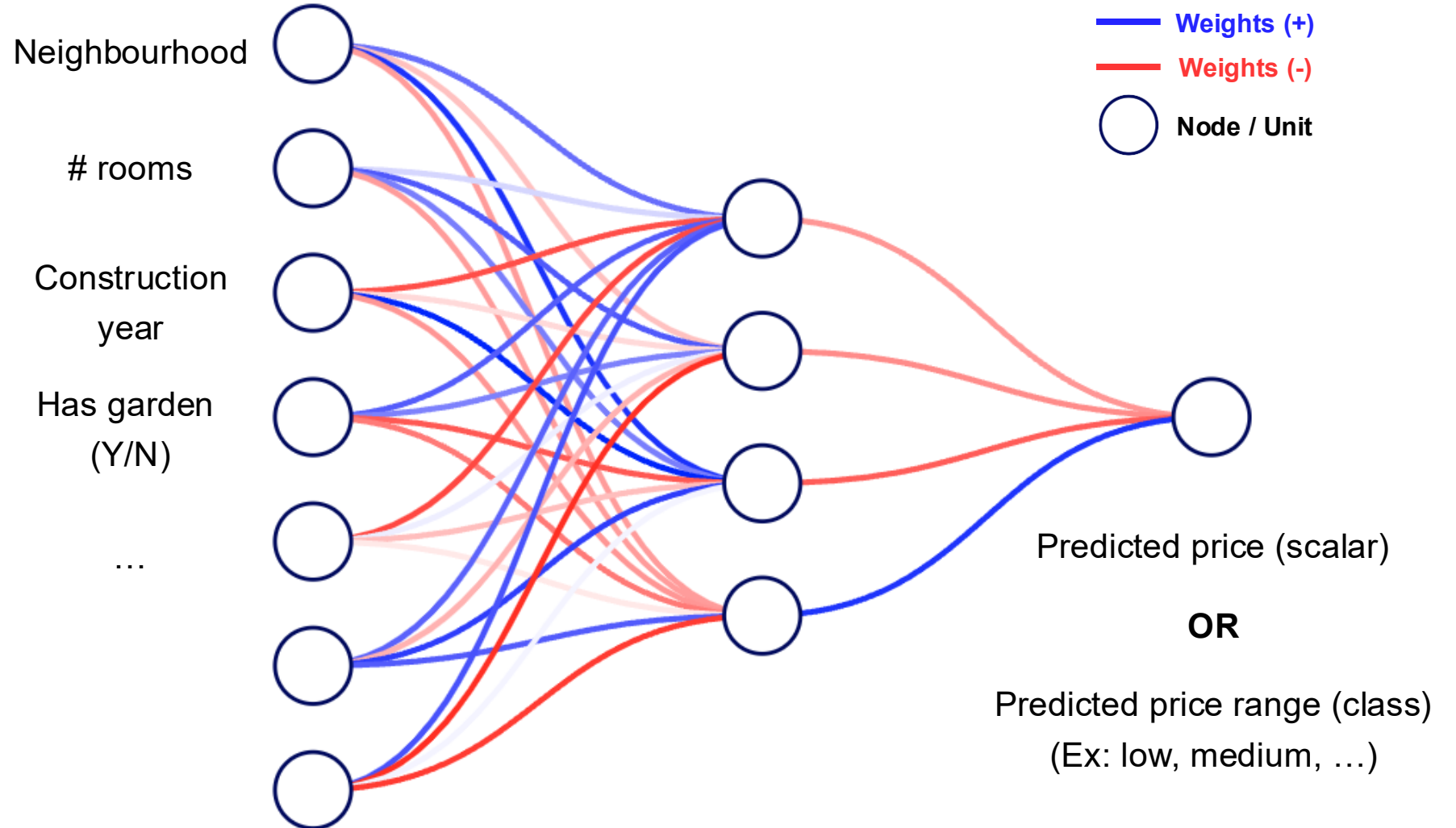
# Recap: Feed-forward Networks (FFNs)

Use features to :

- predict (scalar values)
- classify (labels)

Ex:

Predict the price of a house based on features



Input Layer  $\in \mathbb{R}^7$

Hidden Layer  $\in \mathbb{R}^4$

Output Layer  $\in \mathbb{R}^1$

# Accelerating your models

- Yesterday we implemented a neural network using Python *for* loops.
- It is good for gaining an intuition for neural networks.
- But it is really not very efficient...

# Accelerating your models

- Python *for* loops are extremely slow.
- For larger models we need to use more efficient implementations.
- Deep learning libraries with C++ backends provide this. For example:
  - PyTorch
  - TensorFlow
  - JAX + NumPy

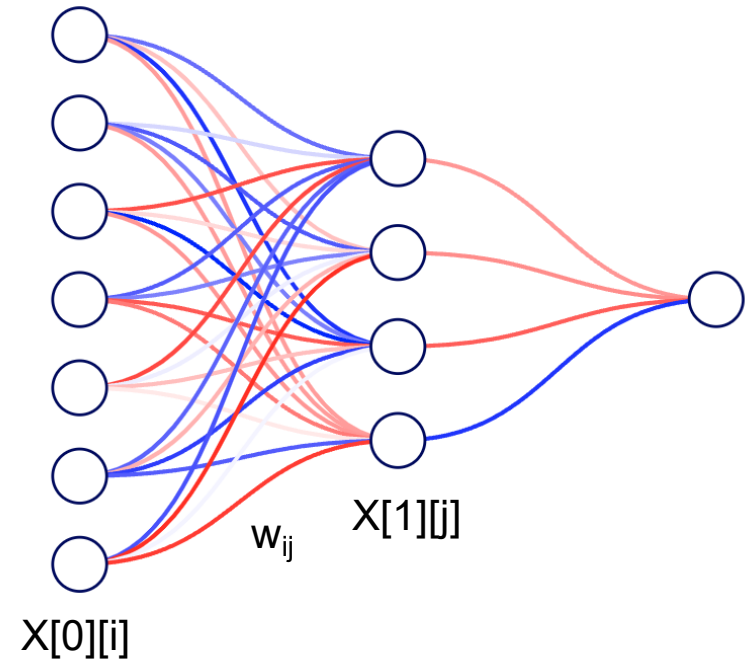
# Accelerating your models

- Python *for* loops are extremely slow.
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- Deep learning libraries with C++ backends provide this. For example:
  - PyTorch
  - TensorFlow
  - JAX + NumPy
- Today's goal: make few but large matrix operations so model training and data processing is more efficient.
- How?
  1. We will use **NumPy** so you understand the impact of matrix multiplications.
  2. And later the vectorization and automatic differentiation (Autograd) capabilities of **PyTorch**.

# Using vectorized matrix operations to speed up processing

- Last time:

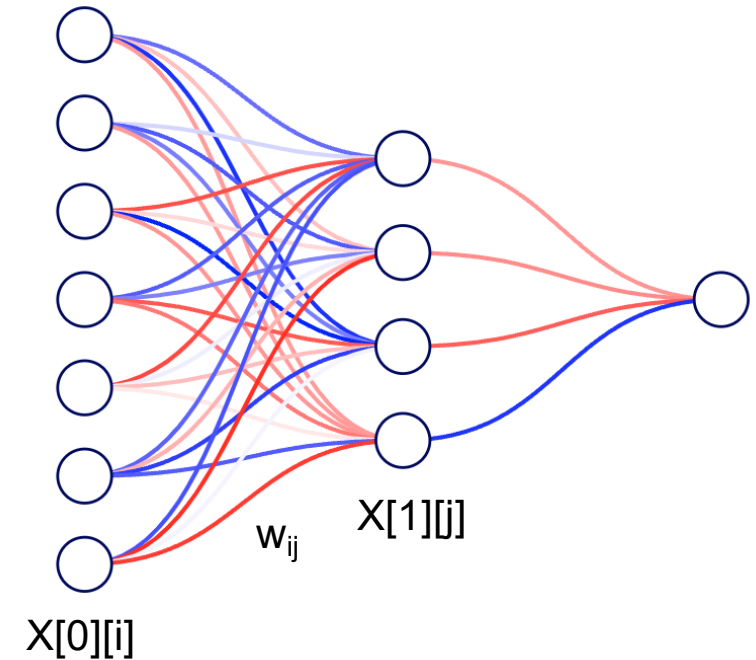
```
def forward(X):  
    for j in range(hidden_layer_dim):  
        z = 0.0  
        for i in range(input_layer_dim+1):  
            z += X[0][i]* w1[i,j]  
        X[1][j] = sigmoid(z)
```



# Using vectorized matrix operations to speed up processing

- Last time:

```
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# Using vectorized matrix operations to speed up processing

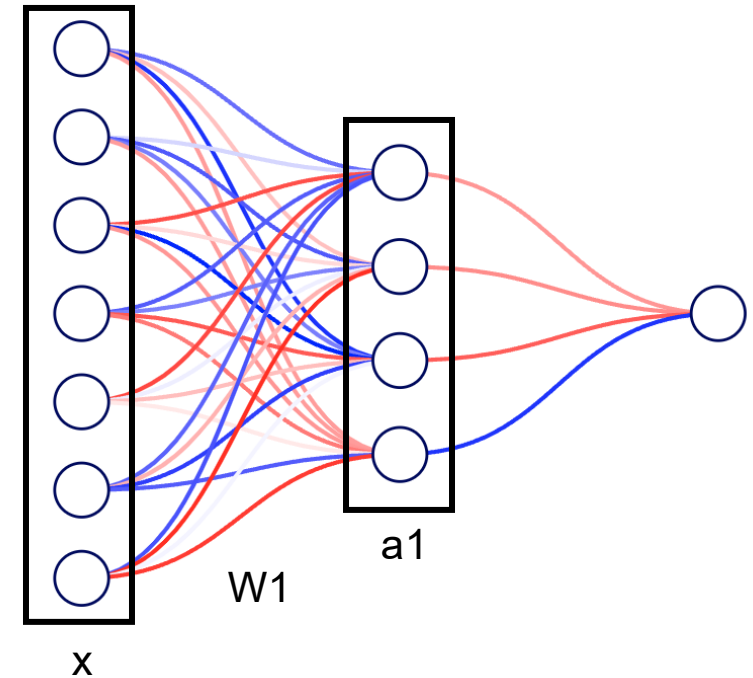
- We can process an input in terms of matrix operations.
- Today:

## NumPy

```
def forward(x):
# First layer
z1 = np.dot(x, W1)
a1 = activation(z1)
```

## PyTorch

```
def forward(self, x):
# First layer
z1 = self.in_layer(x)
a1 = self.hidden_act(z1)
```



$$\begin{matrix}
 x = [x_1 & x_2 & x_3 & x_4 & x_5 & x_6 & x_7] \\
 (1 \times 7)
 \end{matrix}
 \times
 \begin{matrix}
 W_1 = \begin{bmatrix}
 w_{11} & w_{12} & w_{13} & w_{14} \\
 w_{21} & w_{22} & w_{23} & w_{24} \\
 w_{31} & w_{32} & w_{33} & w_{34} \\
 w_{41} & w_{42} & w_{43} & w_{44} \\
 w_{51} & w_{52} & w_{53} & w_{54} \\
 w_{61} & w_{62} & w_{63} & w_{64} \\
 w_{71} & w_{72} & w_{73} & w_{74}
 \end{bmatrix} \\
 (7 \times 4)
 \end{matrix}
 =
 \begin{matrix}
 z_1 = [z_{11} & z_{12} & z_{13} & z_{14}] \\
 (1 \times 4)
 \end{matrix}
 \rightarrow
 \begin{matrix}
 a_1 = g(z_1) \\
 (1 \times 4)
 \end{matrix}$$

# Batching data to speed up processing

- Last time:

```
predictions = []
```

```
for peptide_sequence in dataset:
```

```
    y_pred = forward(peptide_sequence)
```

```
    predictions.append(y_pred)
```

# Batching data to speed up processing

- Last time:

```
predictions = []  
for peptide_sequence in dataset:  
    y_pred = forward(peptide_sequence)  
    predictions.append(y_pred)
```

# Batching data to speed up processing

- We can process batches of data at the same time.
- Today:

predictions = net(dataset)

Encoding of input data (peptides)

ALAKAAAAM	0.9 0.05 0.05 ...
ALAKAAAAN	0.9 0.05 0.05 ..
ALAKAAAAR	
ALAKAAAAT	
ALAKAAAAV	
GMNERPILT	
GILGFVFTM	
TLNAWVKVV	
KLNEPVLLL	
AVVPFIVSV	

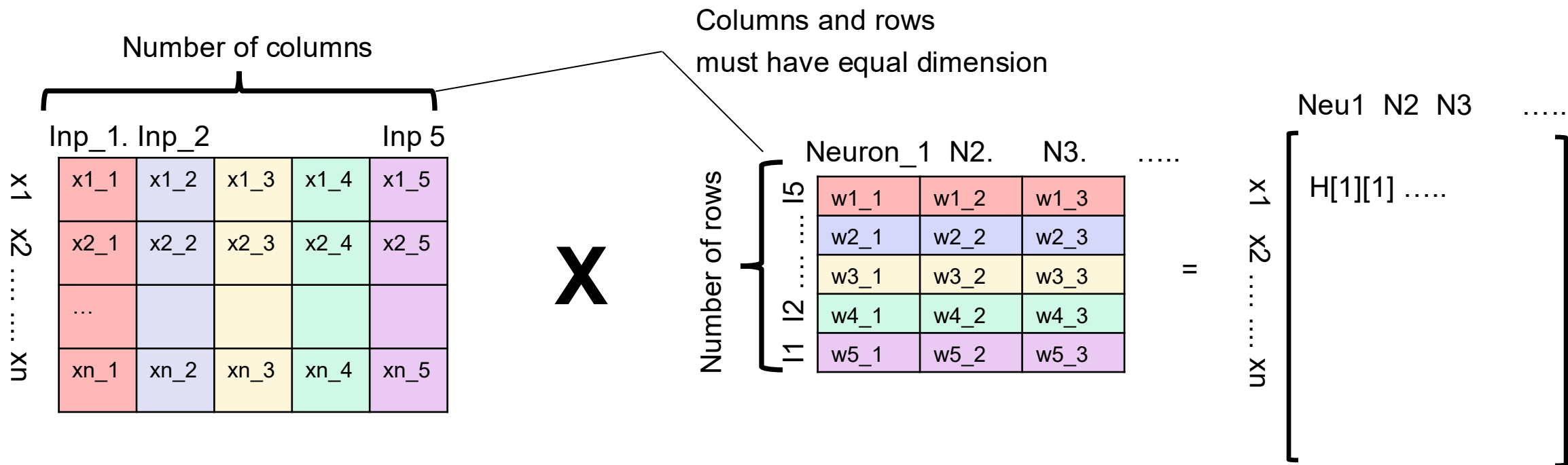
N\_input

x1_1	x1_2	x1_3	x1_4	x1_5
x2_1	x2_2	x2_3	x2_4	x2_5
...				
xn_1	xn_2	xn_3	xn_4	xn_5

N\_datasize/batch

# Batching data to speed up processing

- We can process batches of data at the same time.
- We can apply the weights of all hidden neurons to the input in fewer operations.



- In a **for loop**, each operation is executed **sequentially**, meaning one must finish before the next begins — this is **slow**
- When you **vectorize**, the operations involved in multiplying two matrices can be executed **in parallel**. This is especially effective on GPUs.
- Libraries like **NumPy** and **PyTorch** use highly optimized **C/C++** under the hood to perform these operations **much faster** than pure Python.

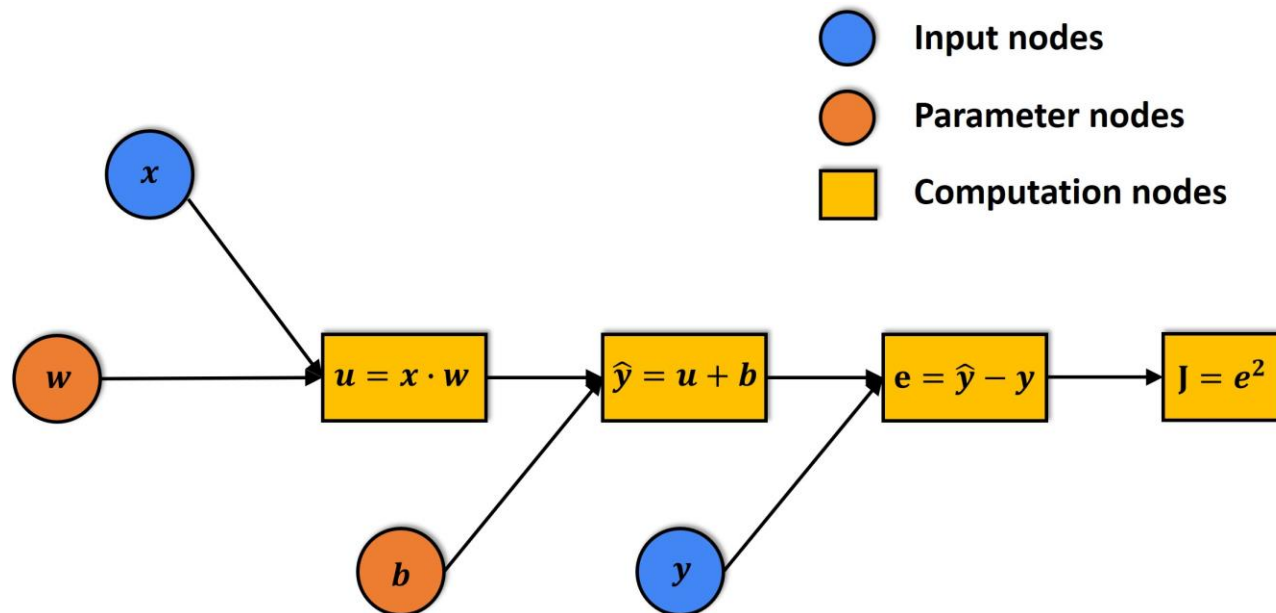
A                      B

$$\begin{array}{c} \boxed{-} \\ \boxed{+} \end{array} \begin{bmatrix} 1 & 2 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 & 1 & 1 & 1 & 1 \\ 2 & 3 & 4 & 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix} \times \begin{bmatrix} 2 & 5 & 1 & 1 & 1 \\ 6 & 7 & 1 & 1 & 1 \\ 1 & 8 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 \end{bmatrix} \begin{array}{c} \boxed{-} \\ \boxed{+} \end{array}$$

$\boxed{-}$   $\boxed{+}$ 
 $\boxed{-}$   $\boxed{+}$

▶ Multiply

Nice online matrix multiplication visualization tool:  
<https://matrixmultiplication.xyz/>



## In PyTorch

```
optimizer.zero_grad()
y_pred = net(x)
loss = criterion(y_pred, y)
loss.backward()
optimizer.step()
```

In practice, the backward pass is usually called on the loss: `loss.backward()`.

# What about peptides which are not 9-mers?

- If all our peptides are 9-mers, FFNN works fine
- However, what about a 12-21mers?
- Need to pad the sequences to the maximum peptide length

CAHHFWTK

TINYTIFK

WMNSTGFTK

YIFWIRTPR

TTTIKPVSYK

WLWGFLSRNK



CAHHFWTKXX

TINYTIFKXX

WMNSTGFTKX

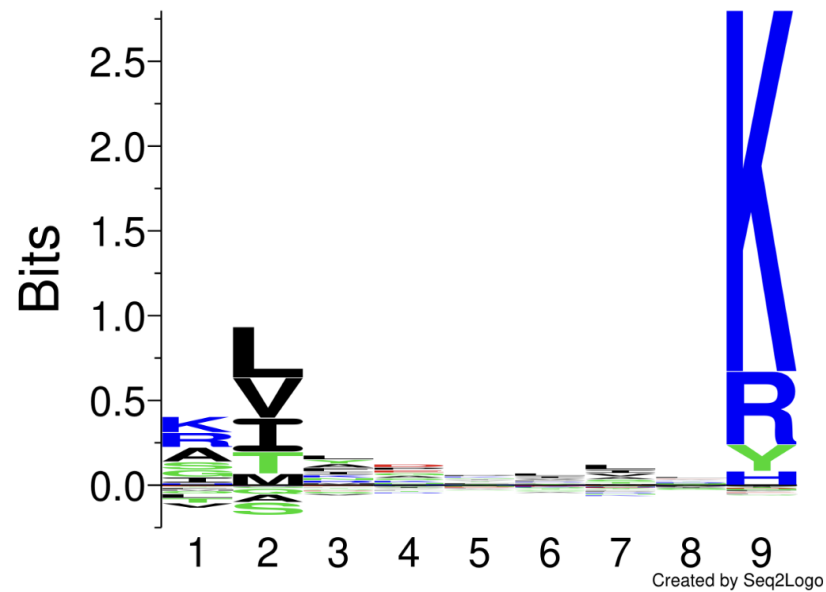
YIFWIRTPRX

TTTIKPVSYK

WLWGFLSRNK

# What about peptides which are not 9-mers?

- However, this padding creates a problem:  
The anchor residues are no longer aligned!



CAHHFWTKXX

TINYTIFKXX

WMNSTGFTKX

YIFWIRTPRX

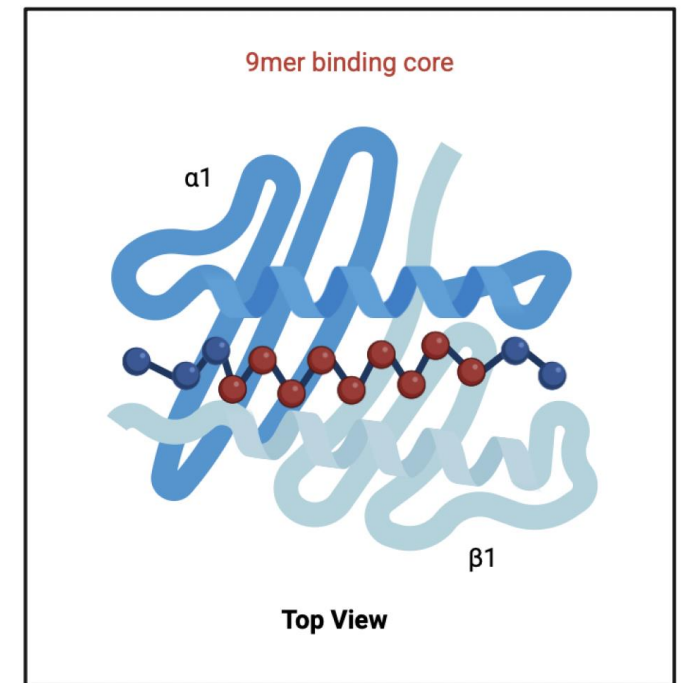
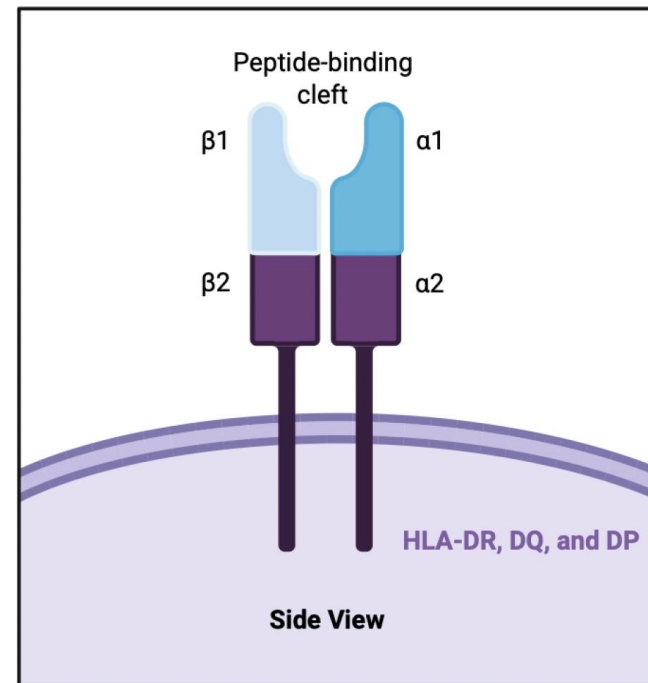
TTTIKPVSYK

WLWGFLSRNK

# What about peptides which are not 9-mers?

- MHC class II peptides are usually longer than 9 amino acids
- Binding is mainly driven by a 9-mer core within the peptide
- The 9-mer core can occur at different positions in the peptide

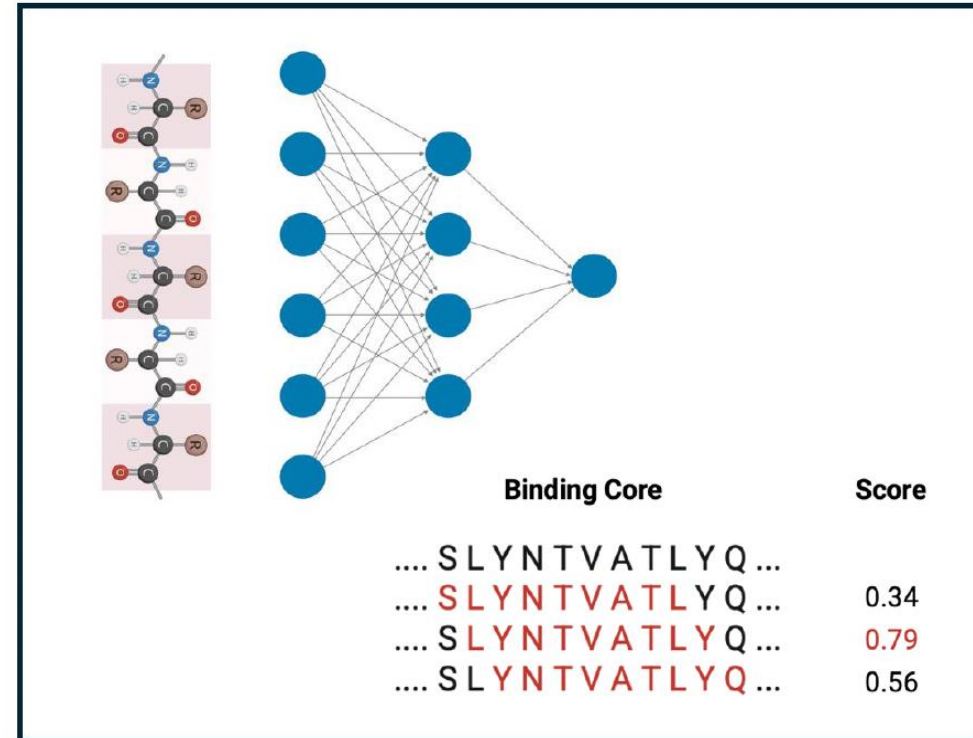
## MHC Class II



# What about peptides which are not 9-mers?

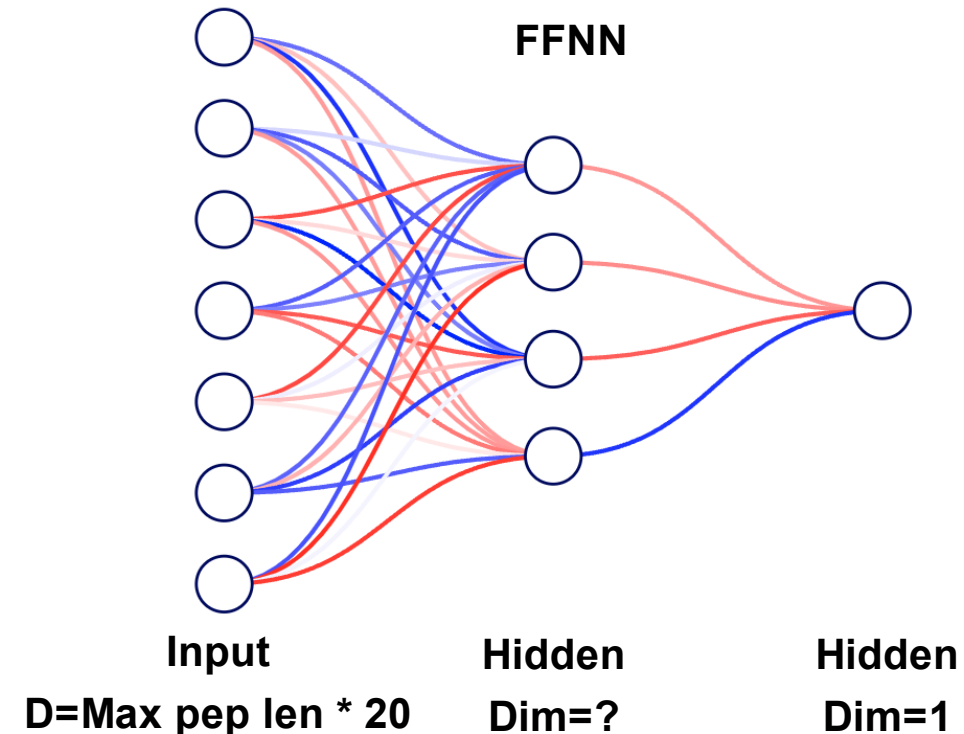
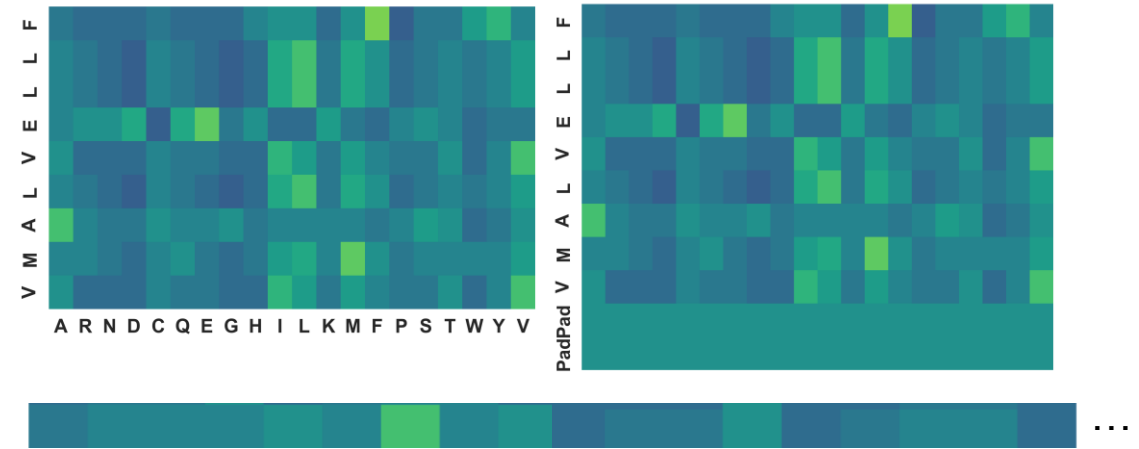
- NNAlign evaluates all possible 9-mer binding cores within each MHC class II peptide during the forward pass
- The peptide score is defined as the highest score among these candidate cores, and backpropagation is performed through the best-scoring 9-mer core.

## NNAlign

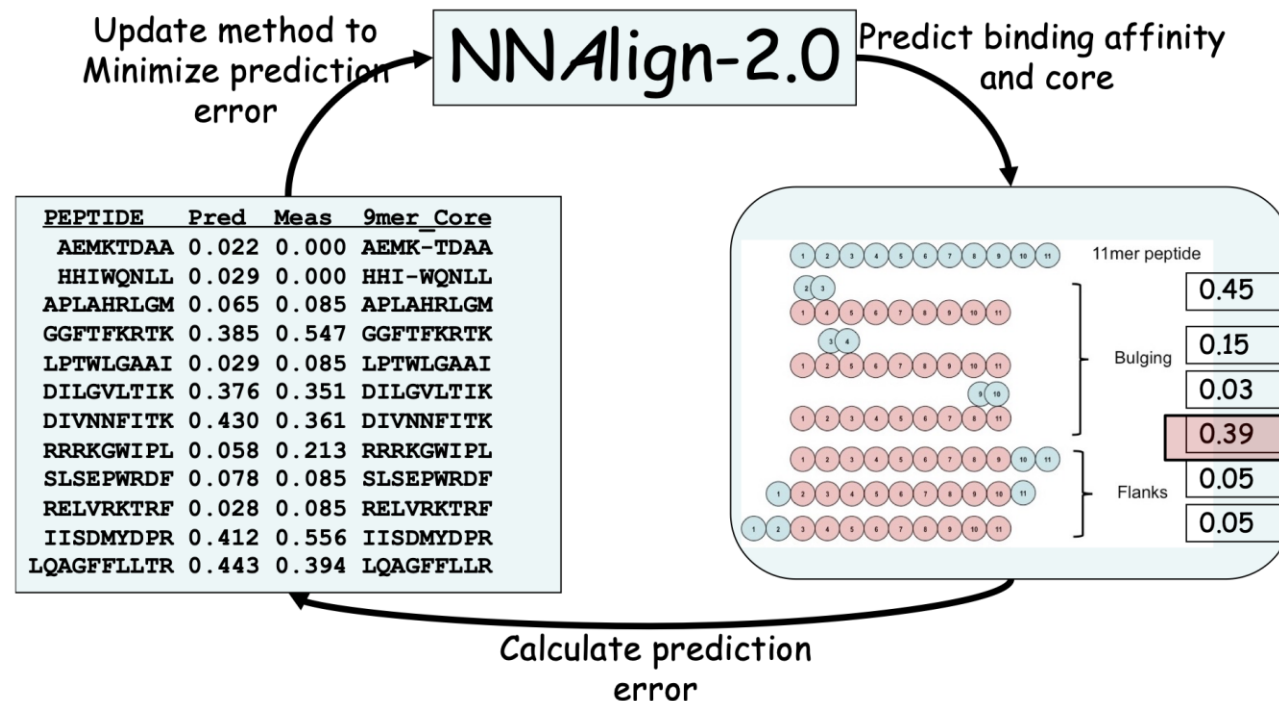


# Part I - FFNN exercise

- Implement an FFNN using efficient matrix multiplication operations.
- Peptides may have different lengths. Shorter sequences must be padded. Why?
- Use a flattened array as input.
- Try to change the learning rate or number of neurons and see if it impacts performance.
- Compare your performance and computation speed with last times NN exercise.



- Implement the forward pass of the NNAlign method
- Compare the performance of the NNAlign method vs standard Feed-forward neural network. Is NNAlign performing better?
- Aside from potential performance gains, what other advantages are there of the NNAlign method's predictions? (hint: interpretability)



**We are here to take your questions.**

(when in doubt: Print output of a given operation and their dimensions of a tensor `x` using `x.shape` or `x.size`)