

**DTU**





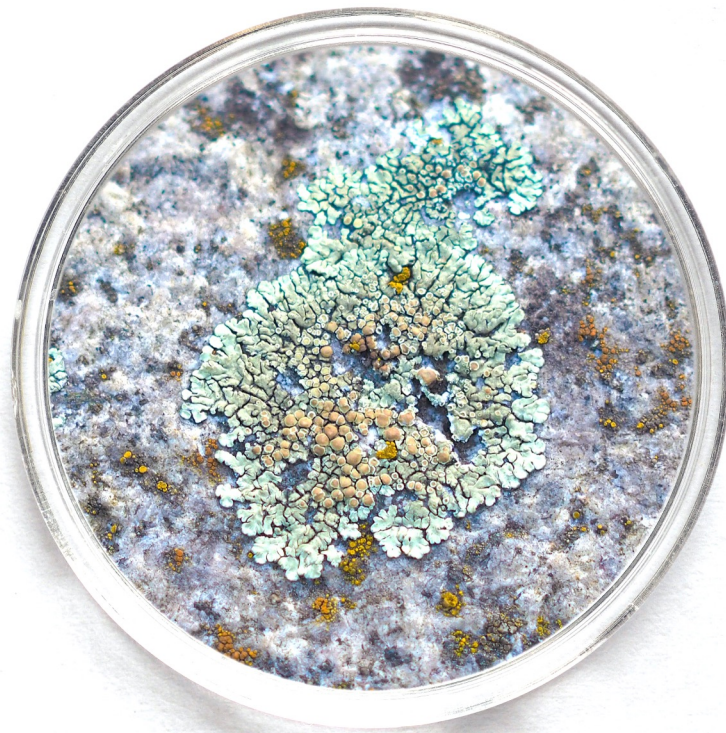
**DTU Health  
Technology  
Bioinformatics**

## ***Quantitative metagenomics***

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*DTU Bioinformatics section*  
Slides adapted from Trine Zachariasen

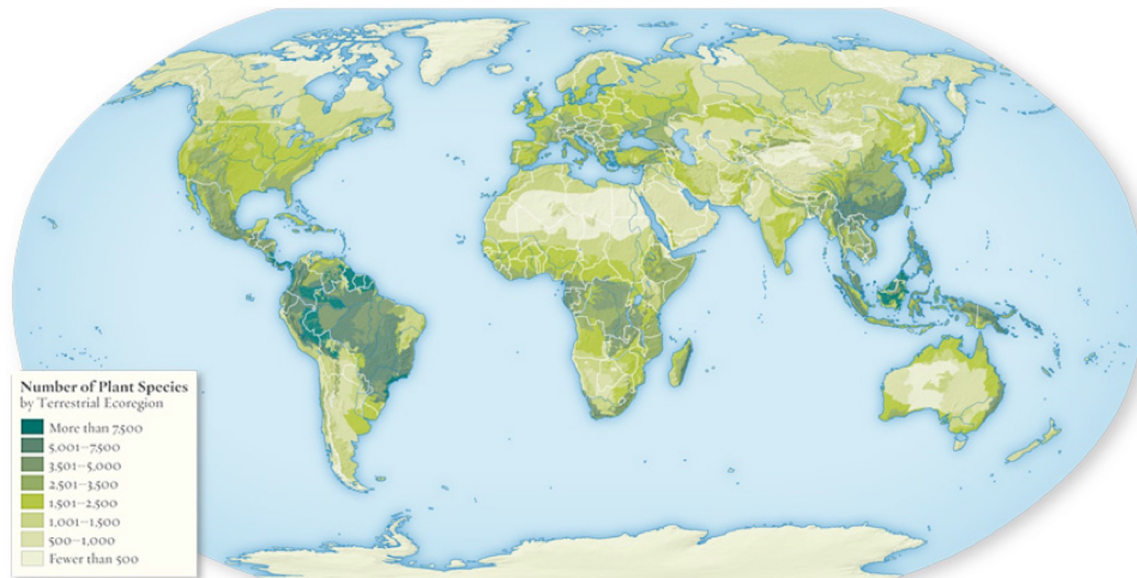
# Menu

- Diversity measurements
  - Abundance
  - Alpha & beta diversity



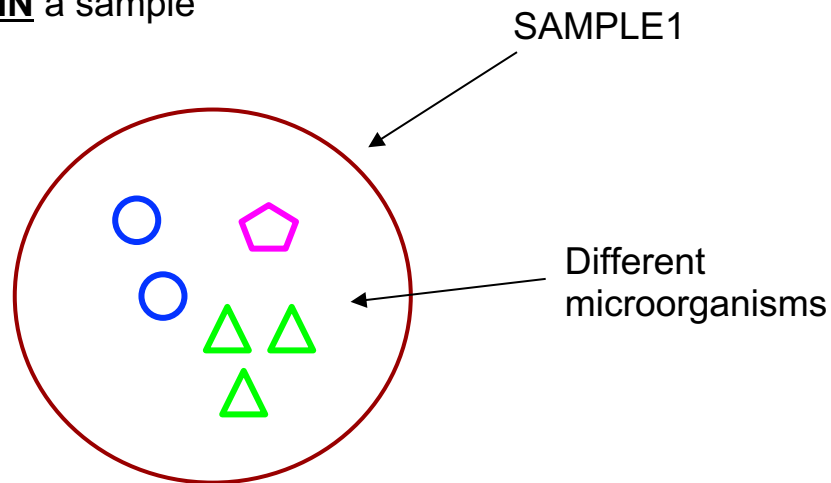
# Classical measures of diversity

- Richness
- Rarefaction
- Diversity
  - Alpha
  - Beta



# Describing biodiversity: Alpha-diversity

Describes the diversity WITHIN a sample



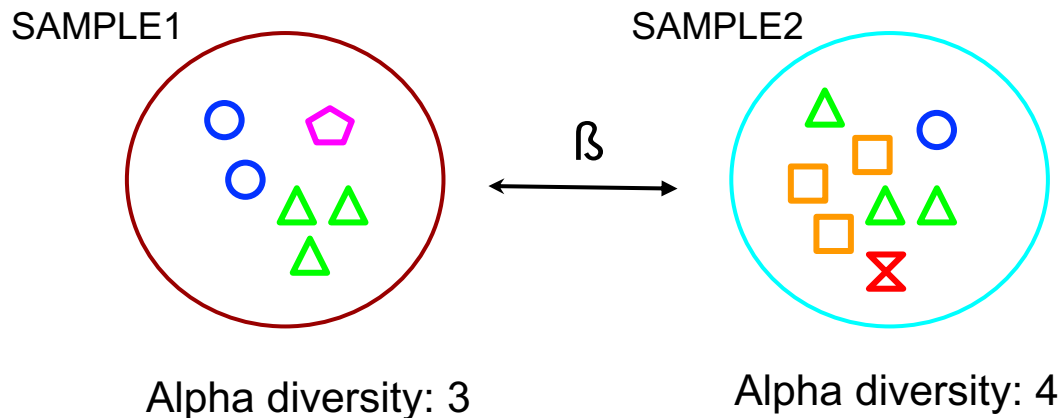
Alpha diversity: 3

# Describing biodiversity: Beta-diversity

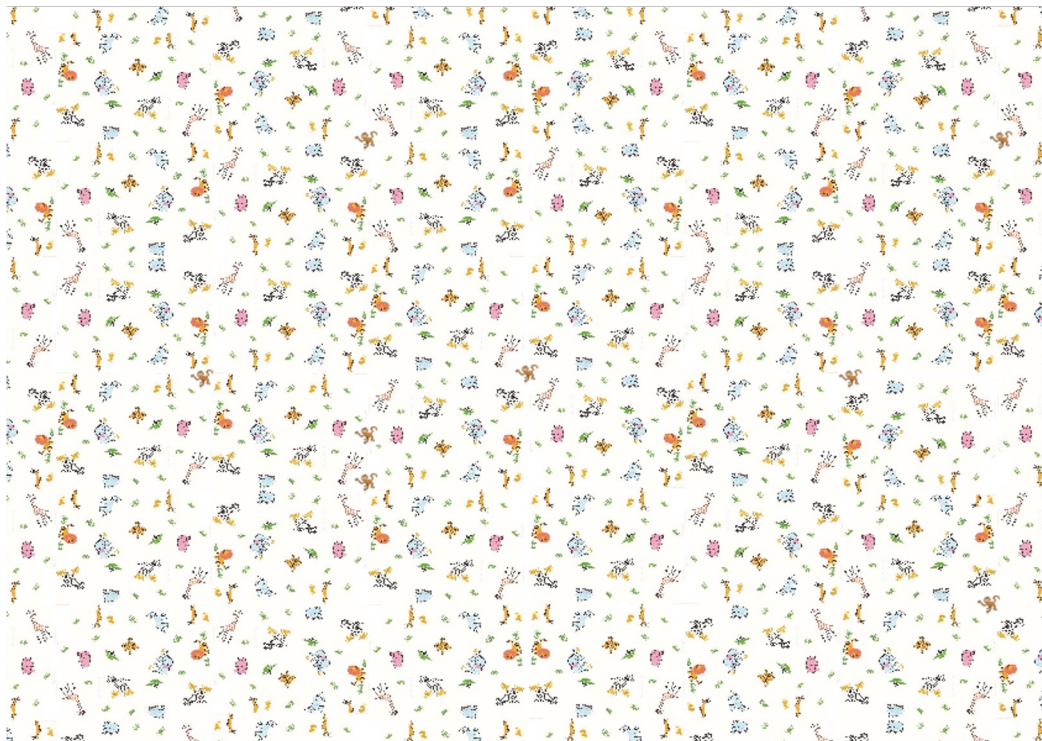
Describes the diversity **BETWEEN** samples,

$$(\alpha_{\text{Sample1}} - c) + (\alpha_{\text{Sample2}} - c) = \beta$$

c = species in common



# Abundance (counts)



Lion	64
Zebra	128
Giraffe	64
leopard	64
rhinoceros	64
hippopotamus	128
gazelle	128
elephant	64
monkey	9

# Species richness

- The number of different species in a system

Lion	64
Zebra	128
Giraffe	64
leopard	64
rhinoceros	64
hippopotamus	128
gazelle	128
elephant	64
monkey	9

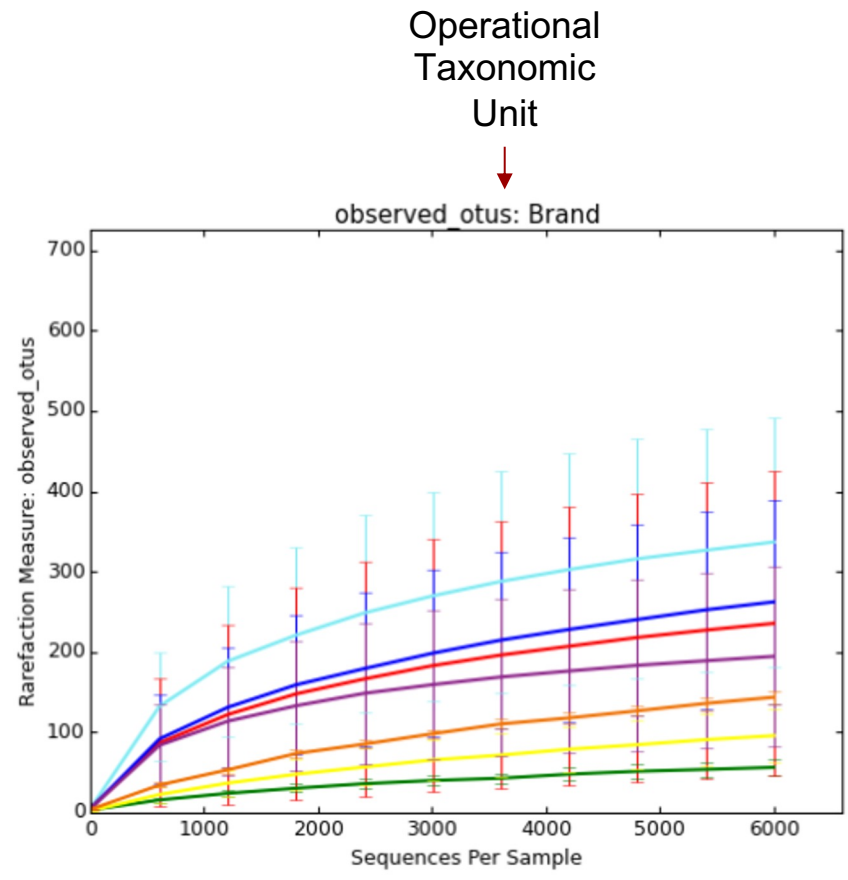


9 observed species



# Rarefaction

- Species richness is a function of our no. observations
- When have we sampled enough?
- Mostly used for 16s rRNA amplicons...why?



# Shannon index

- Incorporates species richness & evenness
- Quantify the entropy (information content)
- Quantifies the uncertainty (degree of surprise)
- The Shannon index increases as both the richness and the evenness of the community increase
- Typical values are generally between 1.5 and 3.5 in most ecological studies, and the index is rarely greater than 4

$$H' = - \sum_{i=1}^R p_i \ln p_i$$

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$$H' = -(\ln p_1^{p_1} + \ln p_2^{p_2} + \ln p_3^{p_3} + \dots + \ln p_R^{p_R})$$

$P_i$  = species proportion

$R$  = observed species = richness

# Shannon index



Lion	1
Zebra	2
Giraffe	1
Leopard	1
Rhinoceros	1
Hippopotamus	2
Gazelle	2
Elephant	1
Monkey	0

$$H' = -(\ln p_1^{p_1} + \ln p_2^{p_2} + \ln p_3^{p_3} + \dots + \ln p_R^{p_R})$$

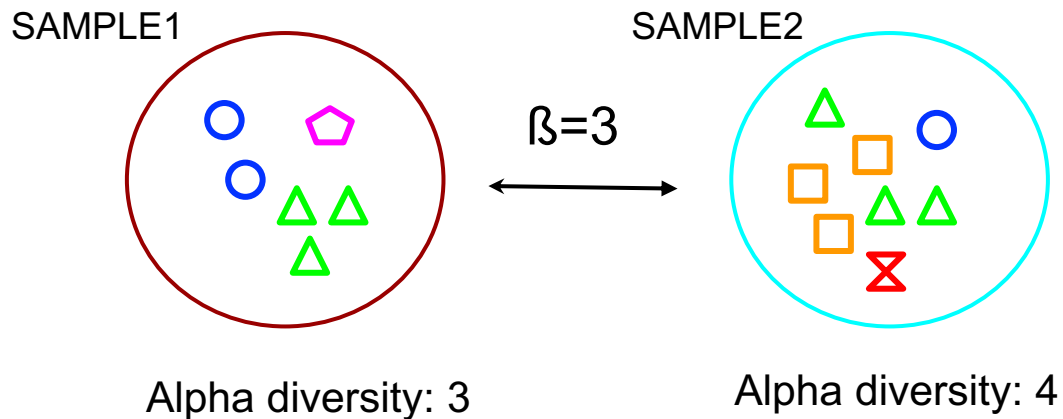
*11 animals (NOT species) meaning each animal is 0.09 of the total abundance*

$$H' = -(\ln(0.09^{0.09}) + \ln(0.18^{0.18}) + \dots) = 2.0$$

# Describing biodiversity: Beta-diversity

$$(\alpha_{\text{sample1}} - c) + (\alpha_{\text{sample2}} - c) = \beta$$

$$(3-2) + (4-2) = 3$$



# Bray-curtis dissimilarity

$$0 \leq B \leq 1$$

$$B_{ij} = 1 - 2C_{ij} / (S_i + S_j)$$

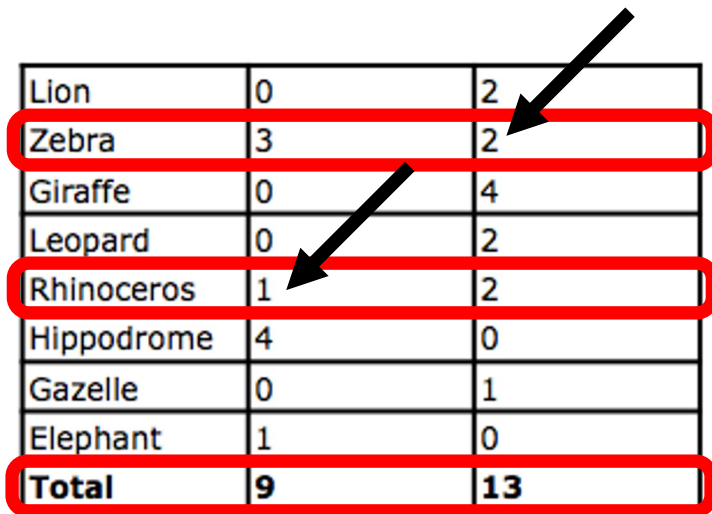
C = sum of the lowest count of all common species

S = total count of the sample

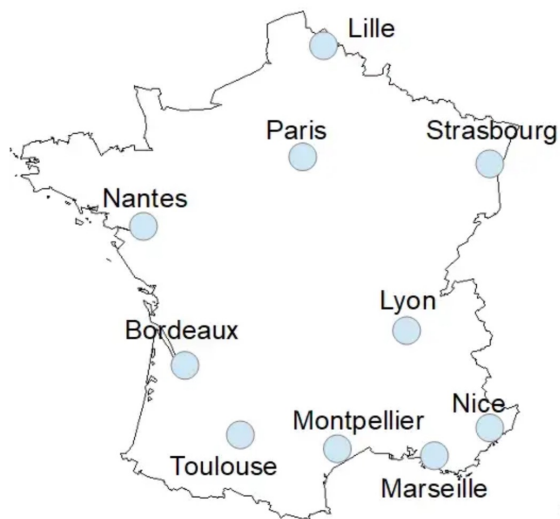
1 means that they do not share anything

$$B_{s_1s_2} = 1 - 2*(2+1) / (9 + 13) = 0.73$$

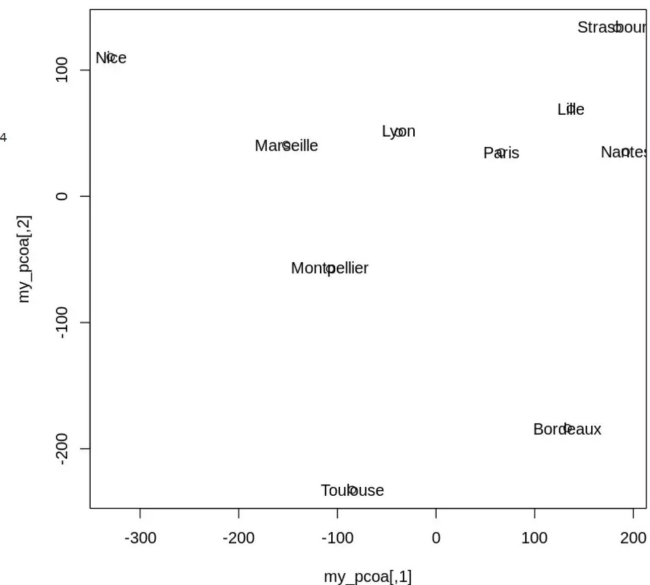
Lion	0	2
Zebra	3	2
Giraffe	0	4
Leopard	0	2
Rhinoceros	1	2
Hippodrome	4	0
Gazelle	0	1
Elephant	1	0
<b>Total</b>	<b>9</b>	<b>13</b>



# PCoA analysis



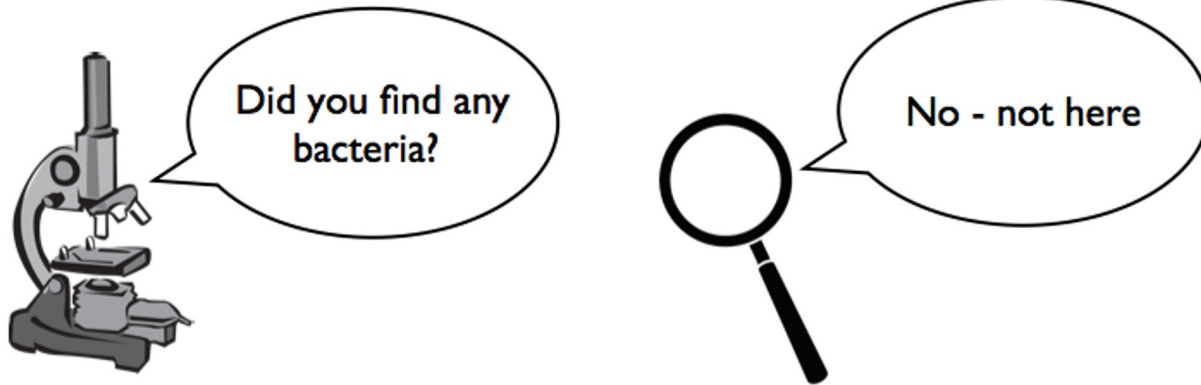
	Paris	Marseille	Lyon	Toulouse	Nice	Nantes	Strasbourg	Montpellier	Bordeaux
Marseille	181								
Lyon	116	99							
Toulouse	265	222	252						
Nice	354	160	271	412					
Nantes	132	401	272	412	539				
Strasbourg	110	335	235	466	542	312			
Montpellier	184	92	103	126	281	385	346		
Bordeaux	131	354	266	123	543	290	312	259	
Lille	64	275	178	383	490	251	189	280	254



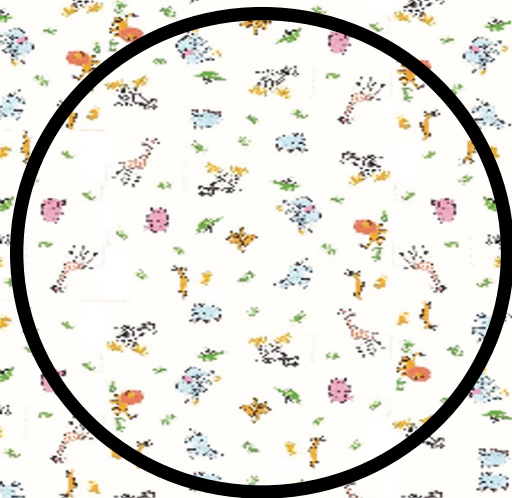
<https://towardsdatascience.com/principal-coordinates-analysis-cc9a572ce6c>

# Sampling effect

- To be fair we should sample equally in the systems we investigate



**Sample sizes**





# Sample sizes

- Accounting for different sample sizes:
  - Normalize to sample size
  - Rarefy (downsize) samples
  - Statistically model the variance

# Normalizing

$$N = n_i/n_{\text{tot}}$$

Lion	64	1
Zebra	128	2
Giraffe	64	1
Leopard	64	1
Rhinoceros	64	1
Hippopotamus	128	2
Gazelle	128	2
Elephant	64	1
Monkey	9	0
<b>Total</b>	<b>713</b>	<b>11</b>

Lion	8.98	9.09
Zebra	17.95	18.18
Giraffe	8.98	9.09
Leopard	8.98	9.09
Rhinoceros	8.98	9.09
Hippopotamus	17.95	18.18
Gazelle	17.95	18.18
Elephant	8.98	9.09
Monkey	1.26	0
<b>Total</b>	<b>100</b>	<b>100</b>

Issue with different sampling power (higher chance of observing rare species) and does not take compositional nature into account

# Downsize / rarefy

Resample x amount of observations

Lion	64	1
Zebra	128	2
Giraffe	64	1
Leopard	64	1
Rhinoceros	64	1
Hippopotamus	128	2
Gazelle	128	2
Elephant	64	1
Monkey	9	0
<b>Total</b>	<b>713</b>	<b>11</b>

Lion	2	1
Zebra	3	2
Giraffe	0	1
Leopard	1	1
Rhinoceros	0	1
Hippopotamus	3	2
Gazelle	1	2
Elephant	0	0
Monkey	0	0
<b>Total</b>	<b>10</b>	<b>10</b>

## Downsize / rarefy

- Select the target depth carefully
- The more reads we keep the more sensitive
- We may have to remove samples with few counts
- We might throw away a lot of data
- Still does not take compositional nature of data into account

## Compositional data

- Arbitrary total
- Sequencing depth never 100%
- Species can co-exist without abundance inter-influences
- Independence between abundance is affected by the capacity of the sequencing instrument
- Sequencing instrument has fixed number of slots

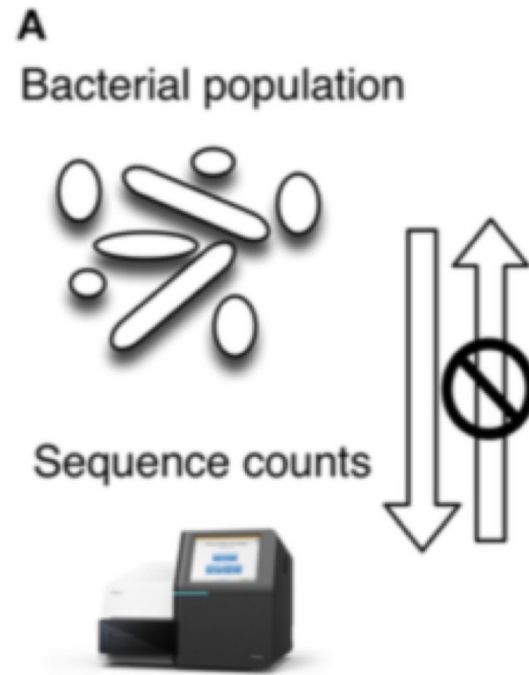
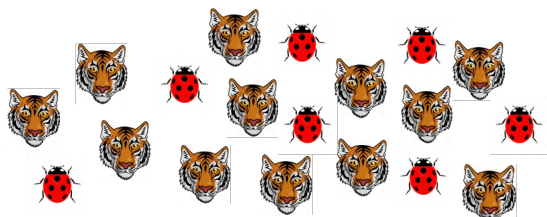


Figure from: Gloor, Gregory B. *et al.*, Microbiome Datasets Are Compositional; And This Is Not Optional. *Frontiers in Microbiology* **8** (2017)

# Compositional data problems

- **Example:** an environment containing both tigers and ladybugs
- The abundances of the two are not affected by each other
- If the abundance of the ladybugs increases some of the slots with tigers must instead be filled by ladybugs
- i.e. the two environmentally independent species are affecting the read count of each other

Population: 12 tigers and 8 ladybugs



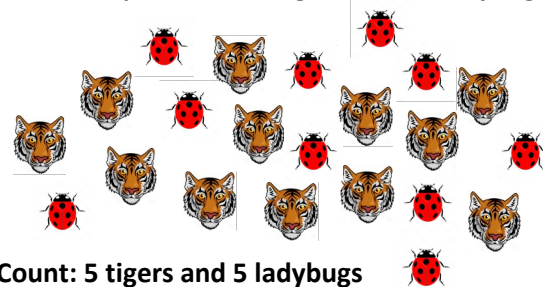
Count: 6 tigers and 4 ladybugs



Increase in abundance of ladybugs,  
no change in abundance of tigers



Population: 12 tigers and 10 ladybugs

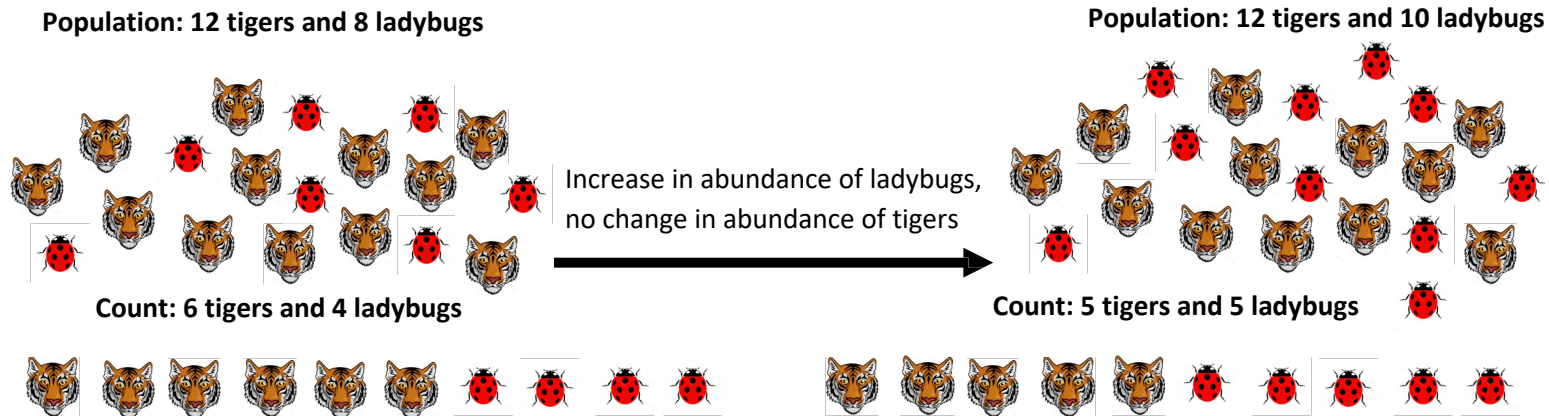


Count: 5 tigers and 5 ladybugs



# Relative abundance

- The counts we get is not the absolute abundance, but their proportions relative to each other



## Dealing with compositional data

- Statistically model the variance & heteroscedasticity
- Use packages developed for RNA-seq such as DESeq2 and edgeR
- DESeq2 takes raw counts divided by sample-specific size factors determined by median ratio of gene counts relative to geometric mean per gene  
([See this link for a brilliant explanation](#))



**If you found it interesting check out the course at  
DTU Food**

23260 Applied methods in metagenomics

